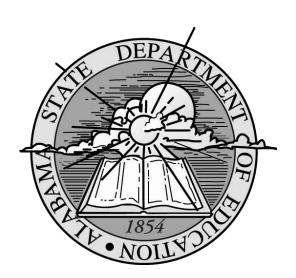
Alabama Reading and Mathematics Test+

Item Specifications

for

Mathematics Grade 6



Alabama State Department of Education Montgomery, Alabama December 2011

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INTRODUCTION

This document provides specific information about the *Alabama Reading and Mathematics Test*⁺ (ARMT⁺). Educators representing each State Board of Education district as well as both city and county school systems served on committees to determine the content standards on which the ARMT⁺ is based. In addition, educators from throughout the state of Alabama served on committees to review the content of the tests, including selecting and reviewing specific mathematics test items, and determining achievement levels.

Teachers must be familiar with the information in this document so that they may incorporate effective teaching of the mathematics content standards with classroom assessments. Using classroom assessments with similar test formats from time to time will help to enable students to demonstrate proficiency on the various content standards in mathematics.

Three item types are included in the ARMT⁺. Multiple-choice, gridded, and open-ended items assess student performance on the ARMT⁺ in mathematics. Multiple-choice items and gridded items carry a point value of 1, while open-ended items carry a point value of 3. In this document, teachers will see representative item types for each mathematics content standard.

Content Standard A statement of what students should know

and be able to do by the end of the academic

year

Item Type Multiple-choice, gridded, open-ended items

Additional Information Further information about the test items for

the content standard

Sample Items A collection of item types for each content

standard

Answer Key Answers for multiple-choice items and

gridded items

Scoring Rubrics for Open-Ended Items Scoring guide for open-ended items

CONTENT STANDARDS Grade 6

CONTENT STANDARD		
Number and Operations		
 Demonstrate computational fluency with addition, subtraction, multiplication, and division of decimals and fractions. Solve problems involving decimals, percents, fractions, and proportions. 	9 <u>12</u> 21	
Algebra		
3- Solve problems using numeric and geometric patterns.	5 5	
Geometry		
 4- Identify two-dimensional and three-dimensional figures based on attributes, properties, and component parts. 5- Plot coordinates on grids, graphs, and maps. 	5 <u>4</u> 9	
Measurement		
6- Classify angles as acute, obtuse, right, or straight.7- Solve problems involving perimeter and area of parallelograms and rectangles.	4 6	
 8- Determine the distance between two points on a scale drawing or map using proportional reasoning. 9- Convert units of length, weight, or capacity within the same system 	4	
(customary or metric).	$\frac{4}{18}$	
Data Analysis and Probability		
10- Interpret information from bar graphs, line graphs, and circle graphs.11- Find the probability of a simple event.	6 4 10	
TOTAL POINTS POSSIBLE	63	

ITEMS BY CONTENT STANDARD

DIRECTIONS (These are the directions read by students and the test administrator for Part 1.)

Read the problem and find the answer.

Calculators may *not* be used for Part 1 of the test.

If the problem has a multiple-choice answer, darken the bubble in the correct space in your answer document.

If the problem has an answer grid:

- Write your answer in the boxes at the top of the grid.
- Darken the correct bubble of the number or symbol in the column below.

If your answer is a repeating decimal, round to the nearer hundredth.

For the problems that ask you to show your work, use the space given in your answer document.

• Be sure to show all of your work or explain how you got your answer in the space given.

For all problems, be sure to check your answers.

ITEMS BY CONTENT STANDARD

There are no written directions for Part 2. The directions will be given orally by the test administrator.

DIRECTIONS (These are the directions read by students and the test administrator for Part 3.)

Read the problem and find the answer.

Calculators may be used for Part 3 of the test.

If the problem has a multiple-choice answer, darken the bubble in the correct space in your answer document.

If the problem has an answer grid:

- Write your answer in the boxes at the top of the grid.
- Darken the correct bubble of the number or symbol in the column below.

If your answer is a repeating decimal, round to the nearer hundredth.

For the problems that ask you to show your work, use the space given in your answer document.

- Be sure to show all of your work or explain how you got your answer in the space given.
- If you use your calculator to get your answer, explain the steps you take.

For all problems, be sure to check your answers.

NUMBER AND OPERATIONS

Content Standard 1

Demonstrate computational fluency with addition, subtraction, multiplication, and division of decimals and fractions.

Item Type

Multiple-choice

Additional Information

Mixed numbers or improper fractions may be used. Common and uncommon denominators may be used. Fractions may be in simplest form. No word problems/context problems will be used.

Sample Multiple-Choice Items

 1. $73.51 + 16.02 = \Box$

 57.31 57.49 89.53 90.53

 A B C* D

3. $16.83 - 4.7 = \square$ 30.17 21.53 12.87 12.13

A B C D*

2. $4\frac{2}{7} + 2\frac{3}{7} = \square$ 6 $6\frac{1}{7}$ $6\frac{5}{7}$ $6\frac{5}{14}$

В

Α

 4. $6.4 \times 2.3 = \Box$

 14.72
 8.7
 3.2
 2.2

 A*
 B
 C
 D

D

5. $12 \times \frac{7}{10} = \square$

A $\frac{120}{7}$

C $\frac{1}{2}$

B $\frac{42}{5}$

 $D \quad \frac{2}{7}$

8. $\frac{7}{8}$ $-\frac{1}{3}$

 $\frac{13}{24}$

 $\frac{6}{11}$

 $\frac{8}{11}$

 $\frac{3}{4}$

Δ *

В

C

D

6. $3.12 \div 0.6 = \square$

A 3.76

C 1.872

B 2.52

D 5.2 *

 $9. \quad \frac{3}{4} \div \frac{6}{4} = \square$

 $\frac{7}{24}$

 $\frac{1}{2}$

 $\frac{3}{4}$

 $\frac{9}{9}$

A

B *

C

D

7. $\frac{7}{9} + \frac{7}{18}$

 $1\frac{5}{9}$

A

 $1\frac{1}{6}$

 $\frac{14}{18}$

C

 $\frac{14}{27}$

D

R *

Answer Key

Content Standard 1

Sample Multiple-Choice

- 1. C
- 2. C
- 3. D
- 4. A
- 5. B
- 6. D
- 7. B
- 8. A
- 9. B

NUMBER AND OPERATIONS

Content Standard 2

Solve problems involving decimals, percents, fractions, and proportions.

Item Type

Multiple-choice Gridded Open-ended

Additional Information

Multi-step problems with decimals and/or percents may be used.

Determining discount, sale price, or original price may be required.

Determining amount of interest may be required.

Tables and charts may be used.

Word problems may be used.

Fractions in their simplest form may be required.

Determining ratio or proportion may be required.

Determining the percent of change may be required.

Sample Multiple-Choice Items

(continued on next page)

1. Mr. Miele had enough sugar to make $\frac{3}{4}$ of a batch of cookies. To make a whole batch, he needed $\frac{1}{3}$ cup of sugar.

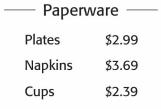


How many cups of sugar did Mr. Miele have?

 $\frac{1}{4}$ $\frac{5}{12}$ $\frac{13}{12}$ $\frac{2}{1}$ **A*** **B C D**

2.

Paper Goods Store



Loraine bought 3 packages of plates and 5 packages of napkins for a party.

If the prices on the sign included tax, how much change should Loraine have received from \$30?

\$2.58 \$6.68 \$23.32 \$27.42 A* B C D

3. Dana recorded the number of days her brother wore sneakers to school and the number of days he wore loafers to school. The ratio of the number of days he wore sneakers to school to the number of days he wore loafers to school was 5 to 2.

If Dana observed and recorded her brother's choice of shoes for 49 days, how many times did he wear sneakers?

2

5

35

C *

A

В

D

56

Sample Gridded Items

1. There are 650 sixth-grade students in the city. Forty-six percent of the students are boys.

How many of the sixth-grade students in the city are boys?

Mark your answer in the answer grid.

2. A digital camera originally cost \$59.95. Its cost decreased 15%.

What is the sale price of the camera, not including tax?

Mark your answer in the answer grid.

3. The science department has a budget of \$400 per year for supplies.

If the science teachers have spent 60% of the supply budget for the year, how much money is left for supplies?

Mark your answer in the answer grid.

5. The price of a shirt was reduced from \$32 to \$24 during a one-day sale. What is the percent of discount on the price of the shirt during the sale?

Mark your answer in the answer grid.

4. Mr. Jennings spent 30% of his gardening budget to purchase rose plants.

If he spent *exactly* \$60, including tax, on rose plants, how much money should he have left over?

Mark your answer in the answer grid.

6. Ashley plans to run a total of 24 miles this week. If Ashley has already run 25% of the total distance, how many more miles does she plan to run this week?

Mark your answer in the answer grid.

Sample Open-Ended Items

This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

- 1. The manager at Ashley's Dress Shop took 10% off the price of all dresses. One month later, the manager took an additional 15% off the price of the same dresses.
 - a. What was the price of a \$120 dress after the first price reduction?
 - b. What was the price of a \$120 dress after the second price reduction?
 - c. Would the price be the same if the store manager simply took 25% off the original price of all the dresses?

This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

- 2. Lauren and Thomas stuffed envelopes for an election campaign. Lauren stuffed 56 envelopes in 5 minutes and Thomas stuffed 42 envelopes in 3.5 minutes.
 - a. How many envelopes did Lauren stuff per hour?
 - b. How many envelopes did Thomas stuff per hour?
 - c. At the same rate of stuffing envelopes, about how long should it take Lauren and Thomas, working together, to stuff a total of 2,604 envelopes?

This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

3. A food server at Harper's Restaurant is paid \$5 per hour plus a 15% tip on the money made on each table he serves.

A food captain at Bea's Fine Dining is paid \$8 per hour plus a 12% tip on the money made on each table he serves.

- a. If the food server at Harper's Restaurant worked 25 hours and the total amount of money made at his tables was \$4,000, what was his total pay for the week?
- b. If the food captain at Bea's Fine Dining worked 25 hours and the total amount of money made at his tables was \$4,000, what was his total pay for the week?

This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

- 4. The band room has 4 kinds of instruments: flutes, trumpets, violins, and drums.
 - a. One-fourth of the instruments are flutes and one-sixth of the instruments are trumpets. What fraction of all of the instruments are flutes and trumpets?
 - b. There are more violins than trumpets. There are more drums than violins. What fraction of the instruments could be violins?
 - c. What fraction of the instruments could be drums?

This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

- 5. Georgie put \$500 in her savings account, earning interest at a rate of 4% each year. She did not make any more deposits or withdrawals.
 - a. How much money was in the account after one year?
 - b. How much money was in the account after 4 years?
 - c. Was the amount of money earned in interest the same or different each year?

This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

- 6. Timothy conducted a survey in which he asked 250 people the number of times they visited a state park last year.
 - a. In Timothy's survey, 20% of the people said they visited a state park exactly 6 times last year. What is the number of people in Timothy's survey that visited a state park exactly 6 times last year?
 - b. In his survey, 110 people said they visited a state park exactly 2 times last year. What percent of people in Timothy's survey visited a state park exactly 2 times last year?
 - c. Timothy said that exactly 43% of the people in his survey never visited a state park last year. Explain why Timothy's statement must be incorrect.

This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

- 7. A computer company expects to increase the number of people it employs at a rate of 4% per year for the next four years.
 - a. If the computer company has 600 employees now, in how many years will it have over 650 employees?
 - b. If the computer company is able to increase the number of people it employs at a rate of 8% per year, when will it have over 650 employees?

This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

- 8. Dan, Jeremy, and Charles each bought 3 jars of salsa for every 4 bags of chips purchased.
 - a. Dan bought 9 jars of salsa. How many bags of chips did he purchase?
 - b. Jeremy bought 20 bags of chips. How many jars of salsa did he purchase?
 - c. Explain why you know that Charles did not purchase 8 jars of salsa.

This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

- 9. Bernie bought a computer for \$900. One year later, the value of the computer was \$720.
 - a. How much did the value of the computer drop?
 - b. What is the percentage of change in the value of the computer?

Show all your work or explain your reasoning *for each part* in the space provided in the answer document.

This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

- 10. James, Caleb, and Abigail bought a pizza. James at $\frac{1}{6}$ of the pizza and Caleb at $\frac{1}{4}$ of the pizza.
 - a. What fraction of the pizza did James and Caleb eat altogether?
 - b. Abigail ate $\frac{2}{5}$ of the pizza that was remaining. What fraction of the original whole pizza did Abigail eat?
 - c. They also bought a pie. James, Caleb, and Abigail shared $\frac{1}{2}$ of the pie. They each had the same fraction of pie. What fraction of the pie did each of them eat?

Answer Key

Content Standard 2

Sample Multiple-Choice

- 1. A
- 2. A
- **3.** C

Sample Gridded

- 1. 299
- 2. \$50.96
- 3. \$160
- 4. \$140
- 5. 25%
- 6. 18

Sample Open-Ended

1. Sample Response(s):

a. $$120 \times 0.10 = $12, $120 - $12 = 108.00

OR

I used my calculator to multiply 120 and 10%, and this gave me a discount of \$12.00. I then subtracted \$12 from \$120. The price of the dress is \$108.00.

OR

I multiplied 120 and 10%. This equaled a discount of \$12.00. After that, I subtracted \$12 from the original dress price of \$120. The price of the dress is now \$108.00.

b. $$108 \times 0.15 = $16.20, $108 - $16.20 = 91.80

OR

I used my calculator to multiply 108 and 15%, and this gave me a discount of \$16.20. I then subtracted \$16.20 from \$108. The price of the dress after the second discount is \$91.80.

OR

I first multiplied \$108 by 15% (0.15). This gave me an answer of \$16.20. Then, I subtracted \$16.20 from \$108. This gave me an answer of \$91.80. This is the price of the dress after the second discount.

c. No, the price would not be the same. If the manager took 25% off the original price of the dress, then the dress would be \$90.00 instead of \$91.80. $($120 \times 0.25 = $30, $120 - 30 = $90.)$

OR

I used my calculator to find that 25% off the original price would be \$90.00 instead of the \$91.80 that was found in **part b**. No, the price would not be the same.

Score Point	Response Attributes
3	All is correct.
2	All logics are correct. OR Two correct logics and correct answers for two problems or drawings. OR One correct logic and correct answers for all problems.
1	One or more answers to problems are correct. OR One correct logic.
0	None correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off task, etc., scored as invalid.)

2. Sample Response(s):

a.
$$\frac{60}{5} = 12$$
; $56 \times 12 = 672$ envelopes

OR

 $\frac{56}{5} = \frac{x}{60}$, $56 \times 60 = 5 \bullet x$, $3,360 = 5x$, $3,360 \div 5 = 672$ envelopes

OR

1 hour equals 60 minutes. There are 12 5-minute intervals in 60 minutes. I multiplied 56 times 12 to get 672 envelopes per hour.

b. $60 \div 3.5 \times 42 = \text{approximately } 720 \text{ envelopes.}$

OR

I used my calculator to figure out how many times 3.5 goes into $60 (60 \div 3.5)$. I then took that answer and multiplied it times 42 to get approximately 720 envelopes per hour.

OR

I found out how many times 3.5 goes into 60 by dividing the two numbers $(60 \div 3.5)$. Then, I took the answer and multiplied it times 42. Thomas stuffed approximately 720 envelopes per hour.

c.
$$672 + 720 = 1,392$$

 $2,604 \div 1,392 = 1.87$

Round up to 2. About 2 hours.

OR

About two hours. Take the answer from **part a** (672) and the answer from **part b** (720) and add these two together (1,392). Then, take 2,604 and divide it by 1,392. This gives an answer of 1.87 which rounds to 2.

OR

I used my calculator to find that it would take about 2 hours to stuff a total of 2,604 envelopes. In my calculator I entered 672 + 720 and got 1,392. I then did $2,604 \div 1,392$ and it gave me an answer of 1.87. I rounded this number up to 2.

Score Point	Response Attributes
3	All is correct.
2	All logic(s) are correct. OR Two correct logics and correct answers for two problems or drawings. OR One correct logic and correct answers for all problems.
1	One or more answers to problems are correct. OR One correct logic.
0	None correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off task, etc., scored as invalid.)

3. Sample Response(s):

a. Harper's Restaurant: $$5 \times 25 = 125 ; $0.15 \times $4,000 = 600 ; \$125 + \$600 = \$725

OR

I used my calculator and multiplied 5 times 25 to get \$125. Then I multiplied 4,000 times 15% (0.15) to get \$600. I then added \$125 and \$600 for a total of \$725.00.

OR

First, I multiplied 5 times 25. This gave me \$125. After that, I multiplied 4,000 times 15% and got an answer of \$600. Then, I added the two answers (\$125 and \$600) and got a total answer of \$725.00. The food server made \$725.00 for the week

b. Bea's Fine Dining: $\$8 \times 25 = \200 ; $0.12 \times \$4,000 = \480 ; \$200 + \$480 = \$680

OR

I used my calculator and multiplied 8 times 25 to get \$200. Then, I multiplied 4,000 times 12% (0.12) to get \$480. I then added \$200 and \$480 for a total of \$680.00.

OR

First, I multiplied 8 times 25. This gave me \$200. After that, I multiplied 4,000 times 12% and got an answer of \$480. Then, I added the two answers (\$200 and \$480) and got a total answer of \$680.00. The food captain made \$680.00 for the week.

Score Point	Response Attributes
3	All is correct.
2	Two logics are correct. OR One correct logic and correct answer to both problems.
1	One or more answers to problems are correct. OR One correct logic.
0	None correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off task, etc., scored as invalid.)

4. Sample Response(s):

a.
$$\frac{1}{4} + \frac{1}{6} = \frac{3}{12} + \frac{2}{12} = \frac{5}{12}$$

Equivalent

b. $\frac{12}{12} - \frac{5}{12} = \frac{7}{12}$, the fraction of violins and drums combined. $\frac{3}{12}$ is $\frac{1}{12}$ greater than $\frac{2}{12}$, so $\frac{3}{12}$ could be the violins (and will likely be the most common answer), and drums are more than violins, so $\frac{4}{12}$ could be drums as $\frac{3}{12} + \frac{4}{12} = \frac{7}{12}$, or the total of violins and drums. The range of potential answers is: $\frac{1}{6}$ < violins < $\frac{7}{24}$

OR

Equivalent

c. $\frac{4}{12}$ could be drums (and will likely be the most common answer), as it is greater than $\frac{3}{12}$ (which is a potential answer for violins from **part b**) and since

$$\frac{4}{12} + \frac{3}{12} + \frac{5}{12} = \frac{12}{12}$$
 or 1.

The range of potential answers is: $\frac{7}{24} < \text{drums} < \frac{5}{12}$

OR

Equivalent

Score Point	Response Attributes
3	All is correct.
	All logics are correct.
2	OR Two correct logics and correct answers for one or more problems.
	OR One correct logic and correct answers for all problems.
	One or more answers to problems are correct without logic.
1	OR One logic is correct.
0	None correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off task, etc., scored as invalid.)

5. Sample Response(s):

a. $$500 \times 0.04 = $20; $500 + $20 = 520

OR

On my calculator, I multiplied 500 times 0.04. Then, I took the answer and added \$500 to get a total of \$520.

OR

First, I multiplied 500 times 0.04. This gave me an answer of 20. Then, I added 20 to 500 and got an answer of \$520. This is how much money that was in the account after one year.

b. To calculate the amount of money Georgie had after 4 years: after 1 year she had $500 \times 0.04 = 20$; 500 + 20 = 520 after 2 years she had $520 \times 0.04 = 20.80$; 520 + 20.80 = 540.80 after 3 years she had $540.80 \times 0.04 = 21.63$; 540.80 + 21.63 = 562.43 after 4 years she had $562.43 \times 0.04 = 22.50$; 562.43 + 22.50 = 584.93

OR

First, I took the answer for the amount of money that was in the account after one year (\$520) and multiplied it times 0.04. Then, I added \$520 to that answer and got an answer of \$540.80. \$540.80 is the amount in the account after 2 years. To find out how much money was in the account after 3 years, I took \$540.80 and multiplied it times 0.04 to get \$21.63. I added \$540.80 and \$21.63 to get an answer of \$562.43. To find out how much was in the account after 4 years, I took the year 3 answer of \$562.43 and multiplied it by 0.04 for an answer of \$22.50. Add \$562.43 and \$22.50 for a final answer of \$584.93.

OR

I used a calculator to find the amount in the account after 4 years. I first took the answer from **part a** and kept multiplying the answer I got by 1.04, 3 times, until I got an answer of \$584.93.

c. The amount of money earned in interest each year was different. For year one it was \$20; for year two it was \$20.80; for year three it was \$22.43; and for year four it was \$22.50.

Score Point	Response Attributes
3	All is correct.
2	All logic(s) are correct. OR Two correct logics and correct answer for two problems. OR One correct logic and correct answers for all problems.
1	One or more answers to problems are correct. OR One correct logic.
0	None correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off task, etc., scored as invalid.)

6. Sample Response(s):

a. $250 \times 0.20 = 50$ (people)

OR

$$250 \times \frac{1}{5} = 50$$

OR

Equivalent

b. $110 \div 250 = 0.44$ or 44%

OR

Equivalent

c. Because 43% of 250 is 0.43×250 which equals 107.5 and one can't have 0.5 or half of a person.

OR

Per parts a and b, it is known that 20% + 44% have visited a state park a certain number of times last year, leaving only 36% to have visited a state park some other number of times, or not at all.

OR

Equivalent

Score Point	Response Attributes
3	All is correct.
2	All logic(s) are correct. OR Two correct logics and correct answer for two problems. OR One correct logic and correct answers for all problems.
1	One or more answers to problems are correct. OR One correct logic.
0	None correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off task, etc., scored as invalid.)

7. Sample Response(s):

a. Year 1: $600 \times 0.04 = 24$; 600 + 24 = 624

Year 2: $624 \times 0.04 = 24.96$; 624 + 24.96 = 648.96

Year 3: $648.96 \times 0.04 = 25.96$; 648.96 + 25.96 = 674.92.

It will take 3 years to have over 650 employees.

OR

I have to find the amount of employees after each year and then find 4% of that number before calculating the next year. Take 600 and multiply it by 0.04 to get 24. Add 24 to 600. Take 624 and multiply it by 0.04 to get 24.96 and add that to 624. Take 648.96 and multiply it times 0.04 to get 25.96. Once you add 648.96 and 25.96 that is over 650, so three years is the amount of time it will take for this company to have over 650 employees.

OR

I used my calculator to find that it will take three years to have over 650 employees. Take 600 and multiply that by 0.04 and add that answer to 600. Continue to take your answer and multiply it by 0.04 until you get at least 650.

b. Year 1: $600 \times 0.08 = 48$; 600 + 48 = 648

Year 2: $648 \times 0.08 = 51.84$; 648 + 51.84 = 699.84

It will take 2 years to have over 650 employees.

OR

To calculate the amount of time before there are 650 employees, I have to find the amount of employees after one year and then find 8% of that number before calculating the next year. For the first year, take 600 and multiply it by 0.08 for an answer of 48. Add 48 to 600, and take that answer and multiply it again by 0.08 for an answer of 51.84. Add 51.84 to 648 for a total of 699.84. It will take two years to have over 650 people.

OR

I used my calculator to find that it will take two years to have over 650 employees. Take 600 and multiply that by 0.08. Then, add that answer to 600. Continue to take your answer and multiply it by 0.08 until you get at least 650.

Score Point	Response Attributes
3	All is correct.
2	Two logics are correct. OR One correct logic and correct answer to both problems.
1	One or more answers to problems are correct. OR One correct logic.
0	None correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off task, etc., scored as invalid.)

8. Sample Response(s):

a. $9 \div 3 = 3$ and $3 \times 4 = 12$ (bags of chips)

OR

Equivalent

b. $20 \div 4 = 5$ and $5 \times 3 = 15$ (jars of salsa)

OR

Equivalent

c. Jars of salsa are purchased 3 at a time. Any number of jars of salsa is always a multiple of 3. 8 is not a multiple of 3.

OR

Equivalent

Score Point	Response Attributes
3	All is correct.
2	All logic(s) are correct. OR Two correct logics and correct answer for two problems. OR One correct logic and correct answers for all problems.
1	One or more answers to problems are correct. OR One correct logic.
0	None correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off-task, etc., scored as invalid.)

9. Sample Response(s):

a. \$900 - \$720 = \$180

OR

On my calculator, I subtracted 720 from 900 to get 180.

OR

To find the amount of decrease from \$900 to \$720, subtract, \$900 - \$720 = \$180.

b.
$$\frac{180}{900} = 0.20$$
 or 20%.

OR

On my calculator, I first divided the amount of change (180) by the original amount (900). After that, I converted the answer (0.20) into a percent to get 20%.

OR

To find the percent of change, divide the amount of change by the original amount, then convert to a percent. So, $\frac{180}{900} = 0.20$ or 20%.

Score Point	Response Attributes	
3	All is correct.	
2	Two logics are correct. OR One correct logic and correct answer to both problems.	
1	One or more answers to problems are correct. OR One correct logic.	
0	None correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off task, etc., scored as invalid.)	

10. Sample Response(s):

a.
$$\frac{1}{6} + \frac{1}{4} = \frac{2}{12} + \frac{3}{12} = \frac{5}{12}$$
 (of the pizza eaten together)

OR

Equivalent

b.
$$1 - \frac{5}{12} = \frac{12}{12} - \frac{5}{12} = \frac{7}{12}$$
 and $\frac{2}{5} \times \frac{7}{12} = \frac{14}{60}$ or $\frac{7}{30}$ (of the original whole pizza)

OR

Equivalent

c.
$$\frac{1}{2} \div 3 = \frac{1}{6}$$
 (of the pie)

OR

$$\frac{1}{2} \times \frac{1}{3} = \frac{1}{6}$$

OR

Equivalent

Score Point	Response Attributes
3	All is correct.
2	All logics are correct. OR Two correct logics and correct answers for one or more problems. OR One correct logic and correct answers for all problems.
1	One or more answers to problems are correct without logic. OR One logic is correct.
0	None correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off task, etc., scored as invalid.)

ALGEBRA

Content Standard 3

Solve problems using numeric and geometric patterns.

Item Type

Multiple-choice Gridded

Additional Information

Pictures or objects may be used.

Determining a rule may be required.

Tables and charts may be used.

Word problems and problems in context may be used.

Fractions may be used.

Sample Multiple-Choice Items

1. The table below shows the amount of money Susan collected for a charity each week.

Susan's Collections

Week	Amount Collected		
1	\$5		
2	\$12		
3	\$19		
4	\$26		

If the pattern shown in the table continued to increase by the same amount each week, how much should Susan have collected for charity in the ninth week?

\$33	\$40	\$47	\$61
A	В	C	D *

2. Serena used 144 as the first term in a pattern. To get terms after the first, she used the rule "divide by 2, divide by 3, divide by 4, etc."

If Serena continued her pattern according to the same rule, which term should she have written next?

30 5 1.5 1.2 A B C D* 3. The table below shows the amount of money Tim has saved by the end of each week.

Tim's Savings

Week	Amount Saved	
1	\$4.00	
3	\$7.50	
4	\$9.25	
5	\$11.00	
9	\$18.00	

If the pattern continues, how much money should Tim save each week?

В

\$1.75 \$2.00

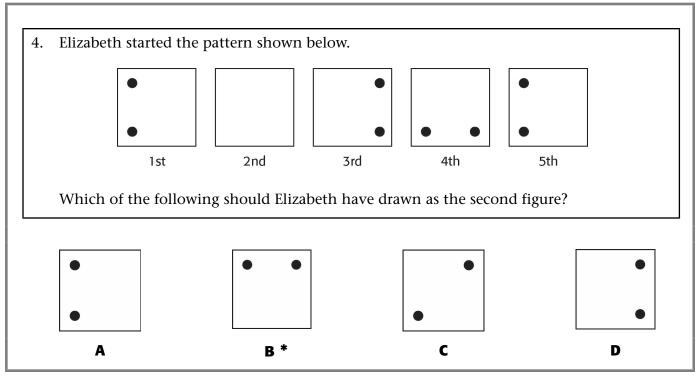
00 \$2.50

C

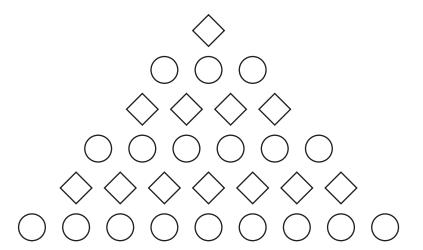
\$7.00

D

A *

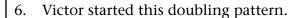


5. Miriam created the tile pattern shown below.



If the pattern continues, how many diamonds and circles should be in the next two rows in the pattern?

- **A** 10 diamonds, 11 circles
- **B** 10 diamonds, 12 circles *
- **C** 11 diamonds, 12 circles
- **D** 11 diamonds, 13 circles





If the pattern continues as shown, how many dots should Victor draw in the next figure?

10 12 16 24

A B C* D

7. The table below shows the number of cars Mario bought and the total amount spent. Each toy car has the same value.

Mario's Tov Cars

Mario 9 10y Cars			
Number of	Total Cost in		
Cars	Dollars		
5	\$4.50		
10	\$9.00		
15	\$13.50		

If the pattern continued as shown in the table, what would be the total cost of 21 of these toy cars?

\$0.90 \$18.00 \$18.90 \$22.50 **A B C** * **D**

8. Jordan started the number pattern below.

0.489, 0.448, 0.407, 0.366, __

If the pattern continues as shown, which of the following rules should he use to find the next term in the number pattern?

- **A** Subtract 0.041 *
- **B** Add 0.041
- **C** Add 0.41
- **D** Subtract 0.41

9. The table below shows the number of minutes volunteers read to a kindergarten class.

Volunteer Readers

Week	Number of Minutes	
1	35	
2	36	
3	39	
4	44	
5		
6	?	

If the pattern continues, how many minutes should the volunteers read to the kindergarten class during week 6?

48	54	58	60
A	В	C	D *

Sample Gridded Items

1. A local radio station plans to give away 2 concert tickets on Monday, 6 concert tickets on Tuesday, and 18 concert tickets on Wednesday.

If this pattern continues, how many concert tickets will the radio station give away on Friday?

Mark your answer in the answer grid.

2. A pattern of 31 shapes appears on the border of an office building. The first 4 shapes of the pattern are shown below.



If the 4 shapes above keep repeating in this order, how many triangles are in the pattern?

3. Ashley's school collected pennies for 8 days to fund a college scholarship. On the first day, Ashley brought 1 penny, the second day she brought 2 pennies, the third day she brought 4 pennies, and the fourth day she brought 8 pennies.

If the pattern continued with the number of pennies doubling on each consecutive day, how many total pennies did Ashley bring after 8 days?

Mark your answer in the answer grid.

4. Jesse decorated an award plaque by drawing a pattern of geometric figures. The first 5 shapes of his pattern are shown below.



If Jesse repeats the pattern in the order shown until there are 13 squares and 14 triangles, how many figures did he draw in his entire pattern?

5. It takes Darren 8 minutes to prepare his supplies to make 6 bracelets. Each bracelet will take 5 minutes to make.

What is the *least* amount of time, in minutes, it will take Darren to prepare his supplies and make 6 bracelets?

Mark your answer in the answer grid.

6. Kris made the pattern shown below.

If the pattern continues, what should be the 11th number in the pattern?

Answer Key

Content Standard 3

Sample Multiple-Choice

- 1. D
- 2. D
- 3. A
- 4. B
- 5. B
- 6. C
- **7.** C
- 8. A
- 9. D

Sample Gridded

- 1. 162
- 2. 8
- 3. 255
- 4. 34
- 5. 38
- 6. 49

GEOMETRY

Content Standard 4

Identify two-dimensional and three-dimensional figures based on attributes, properties, and component parts.

Item Type

Multiple-choice

Additional Information

Matching a net to a three-dimensional figure may be required. Diagrams of two-dimensional figures or three-dimensional figures may be used. Word problems/real-life situations may be used.

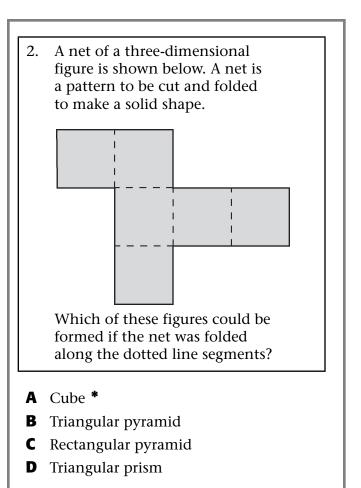
Sample Multiple-Choice Items

1. Gretta drew the figure below.



Which of these names the figure Gretta drew?

- A Rectangular prism
- **B** Triangular prism
- C Triangular pyramid
- **D** Square pyramid *

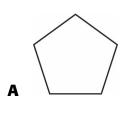


- 3. Which regular figure has only 6 congruent angles?
- **A** Triangle
- C Hexagon *
- **B** Pentagon
- **D** Octagon
- 4. Which figure *always* has 4 congruent sides and *exactly* 2 sets of parallel sides?
- **A** Trapezoid
- C Rhombus *
- **B** Rectangle
- **D** Parallelogram
- 5. Tek has a figure with *exactly* one rectangular base.

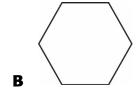
Which of the following could be the shape of Tek's figure?

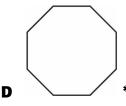
- **A** Triangular prism
- **B** Rectangular prism
- **C** Triangular pyramid
- **D** Rectangular pyramid *

6. Which of the following figures is an octagon?









7. Lyle designed a garden so that it had seven equal sides.

Which figure has *exactly* 7 sides of equal length?

- A regular pentagon
- **B** A regular heptagon *
- **C** A regular nonagon
- **D** A regular decagon

- 8. Which of the following figures *always* has 4 congruent sides?
- A Isosceles trapezoid
- **B** Parallelogram
- **C** Rectangle
- **D** Rhombus *

- 10. Which of the following two-dimensional figures has *exactly* 5 sides?
- **A** Parallelogram
- **C** Hexagon
- **B** Pentagon *
- **D** Octagon

9. April made a sign with exactly one set of parallel sides and exactly one set of congruent sides.

Which could be the shape of the sign?

- A Isosceles trapezoid *
- **B** Isosceles triangle
- **C** Regular quadrilateral
- **D** Regular triangle

11. Henry cut a piece of cardboard into different-shaped pieces. One of the pieces had *exactly* 2 sets of parallel sides and 4 congruent angles.

Which could be one of the pieces Henry cut?

- A A trapezoid
- **B** A rhombus
- **C** A square *
- **D** A pentagon

12. Alyssa drew the picture of the three-dimensional figure below.



Which of the following names the figure Alyssa drew?

- A Cone *
- **B** Cylinder
- **C** Pyramid
- **D** Sphere

14. Albert drew several three-dimensional figures.

Which of the following figures had *exactly* 5 faces and 5 vertices?

- A Triangular pyramid
- **B** Triangular prism
- C Rectangular pyramid *
- **D** Rectangular prism

13. Gabriella drew a picture of a swimming pool. The swimming pool had five sides.

Which is the shape of the swimming pool she drew?

- A Pentagon *
- **B** Parallelogram
- **C** Trapezoid
- **D** Hexagon

Answer Key

Content Standard 4

Sample Multiple-Choice

- 1. D
- 2. A
- 3. C
- 4. C
- 5. D
- 6. D
- 7. B
- 8. D
- 9. A
- 10. B
- 11. C
- 12. A
- 13. A
- 14. C

GEOMETRY

Content Standard 5

Plot coordinates on grids, graphs, and maps.

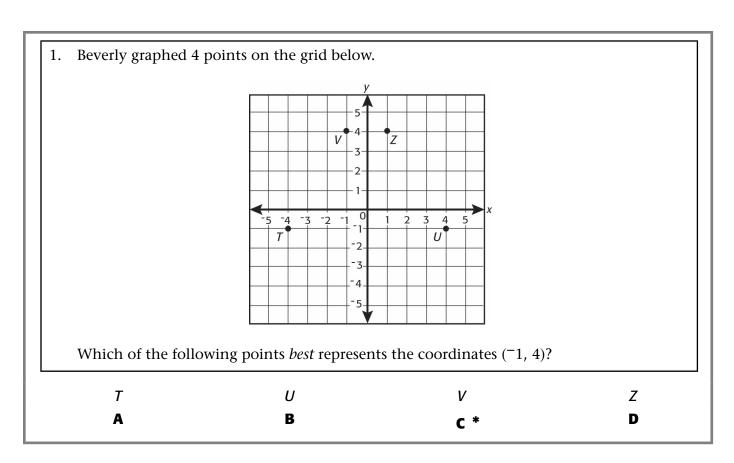
Item Type

Multiple-choice

Additional Information

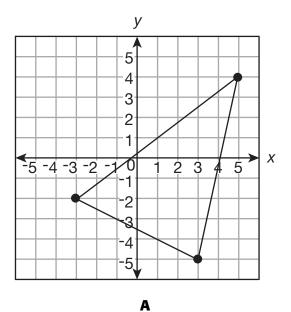
Identifying coordinates of a point on a grid, graph, or map may be required. Following directions to locate a point on a grid, graph, or map may be used. Using ordered pairs to represent the location of a point on a grid, graph, or map may be used. Identifying coordinates of a point on the coordinate plane may be required. Real-life situations may be included.

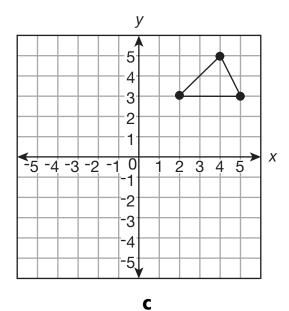
Sample Multiple-Choice Items

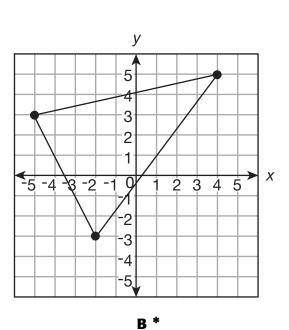


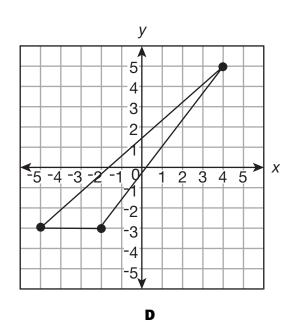
2. Josh made a graph of his newspaper route. He starts at (4, 5), continues to (-5, 3) and (-2, -3), and then returns to where he started.

Which of the following shows Josh's newspaper route?

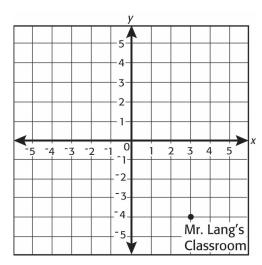








3. The grid below shows the location of Mr. Lang's classroom.



Which best represents the coordinates of Mr. Lang's classroom?

(3, 4)

(3, -4)

 $(^{-}4, 3)$

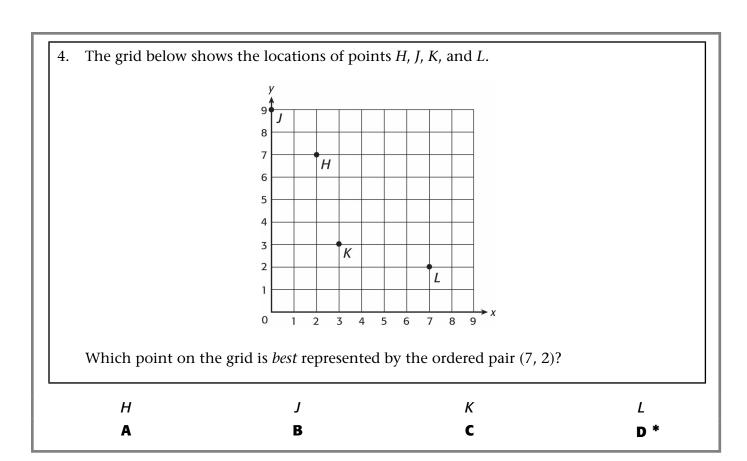
(4, 3)

A

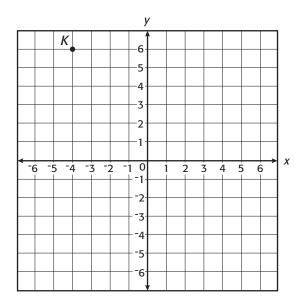
в *

C

D



5. Kendra graphed point *K* on the grid below.



Which ordered pair *best* represents the location of point *K*?

(6, -4)

 $(^{-}4, 6)$

(6, 4)

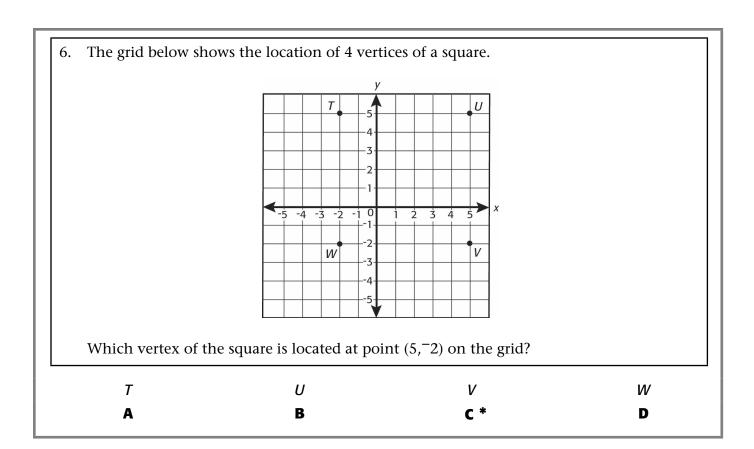
(~4, ~6)

Α

В *

C

D



Answer Key

Content Standard 5

Sample Multiple-Choice

- 1. C
- 2. B
- 3. B
- 4. D
- 5. B
- 6. C

MEASUREMENT

Content Standard 6

Classify angles as acute, obtuse, right, or straight.

Item Type

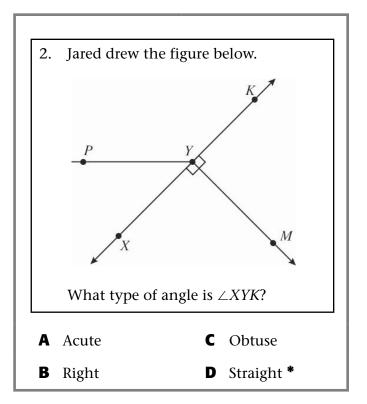
Multiple-choice

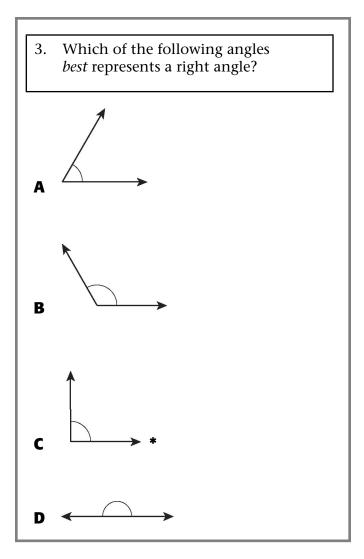
Additional Information

A diagram may be included. Pictures of real-life objects may be included.

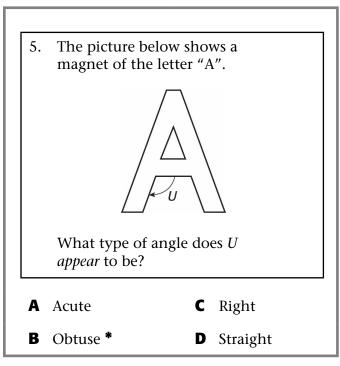
Sample Multiple-Choice Items

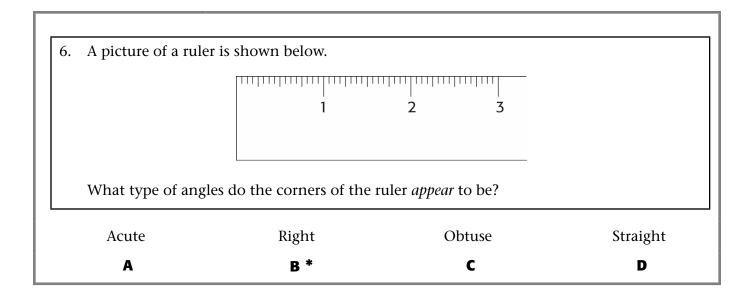
- 1. Mike drew an angle that measured more than 90° but less than 180°. What type of angle did Mike draw?
- **A** Right
- C Obtuse *
- **B** Acute
- **D** Straight





4. Riley rode her bicycle west on Main Street and made a 75-degree turn at Elm Street.
What kind of angle represents the 75° turn Riley made at Elm Street?
A Straight
C Obtuse
B Right
D Acute *



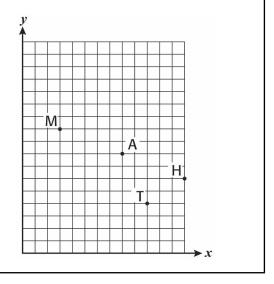


7. Stop signs are constructed in the shape of regular octagons.

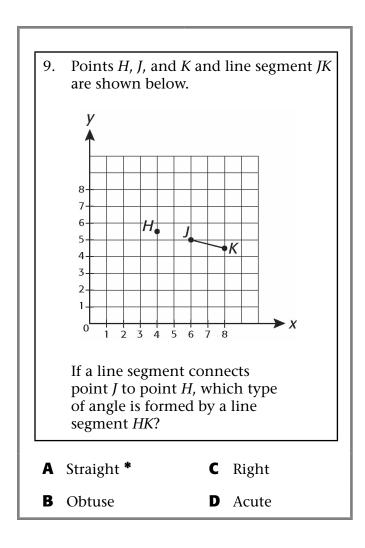
Which of the following angles are at the vertices of a regular octagon?

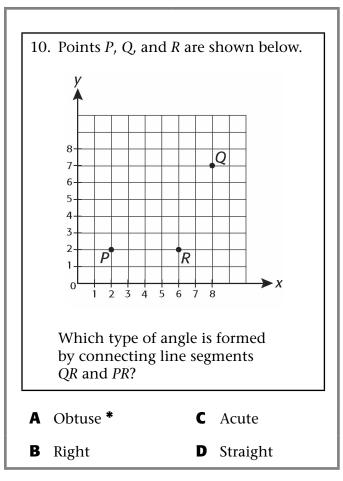
- **A** Acute
- **C** Right
- **B** Obtuse *
- **D** Straight

8. Which type of angle is formed by connecting line segments *MA* and *AT* using point *A* as the vertex?



- **A** Acute
- C Obtuse *
- **B** Right
- **D** Straight





Answer Key

Content Standard 6

Sample Multiple-Choice

- 1. C
- 2. D
- **3.** C
- 4. D
- 5. B
- 6. B
- 7. B
- 8. C
- 9. A
- 10. A

MEASUREMENT

Content Standard 7

Solve problems involving perimeter and area of parallelograms and rectangles.

Item Type

Multiple-choice Gridded Open-ended

Additional Information

Determining a missing measurement when given the area or perimeter of a parallelogram or a rectangle may be required.

Determining either the area or the perimeter of a parallelogram or a rectangle given either the area or the perimeter of the figure may be required.

Diagrams may be used.

Determining the area or perimeter of a shaded part of a figure may be required.

Word problems/real-life situations and problems in context may be used.

A comparison of figures may be required.

Sample Multiple-Choice Items

1.	The front of the door to Rueben's classroom is a rectangle with an area of 2,688 square inches.				
	If the width of the front of the door is 32 inches, what should be the measure of the height?				
	640 inches	116 inches	84 inches	42 inches	

A B C* D

2. The area of a parallelogram is 16 square meters. The base of the parallelogram is 8 meters.

What is the height, in meters, of the parallelogram?

2

8

24

128

A *

В

C

- D
- 3. The perimeter of a square is 20 centimeters.

What is the area?

A 5 sq cm

C 30 sq cm

B 25 sq cm *

D 400 sq cm

5. A diagram of an exercise mat is shown below.

Exercise Mat

8 feet

The width of the mat is $\frac{1}{2}$ the length.

What is the perimeter of the exercise mat in feet?

A 4 feet

C 24 feet *

B 9 feet

D 32 feet

4. The perimeter of a rectangle is 54 inches. The width of the rectangle is 8 inches.

What is the length of the rectangle?

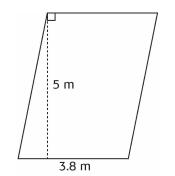
A 16 inches

C 38 inches

B 19 inches *

D 46 inches

5. What is the area of the parallelogram shown below?



A 8.8 sq m

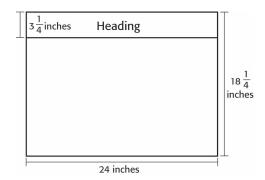
C 19.0 sq m *

B 17.6 sq m

D 38.0 sq m

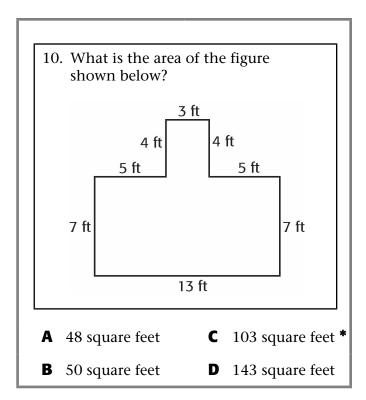
- 7. What is the area of a parallelogram with a width of 13.9 centimeters and a height of 22.4 centimeters?
- **A** 36.3 sq cm
- **C** 72.6 sq cm
- **B** 68.6 sq cm
- **D** 311.36 sq cm *
- 9. What is the perimeter of a parallelogram with sides of 17 inches and 21 inches?
- **A** 4 inches
- C 76 inches *
- **B** 38 inches
- **D** 357 inches

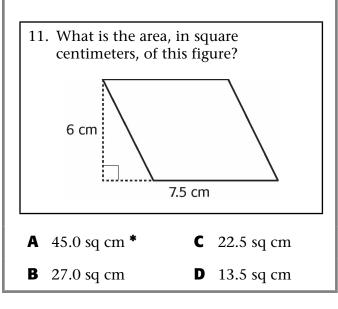
8. A poster on Evan's wall is 24 inches wide and $18 \frac{1}{4}$ inches high. On the top of the poster is a $3 \frac{1}{4}$ inch heading.



What is the perimeter of the poster without the heading?

- **A** 84 inches
- **C** 74 inches
- **B** 78 inches *
- **D** 68 inches





Sample Gridded Items

1. The bottom of the cage where Alex keeps his pet mouse is in the shape of a rectangle with a perimeter of 58 inches. The length of the bottom of the cage is 18.3 inches.

What is the width of the bottom of the cage?

Mark your answer in the answer grid.

2. Sandy removed two small pieces from the large rectangle shown below.

1.5 in.

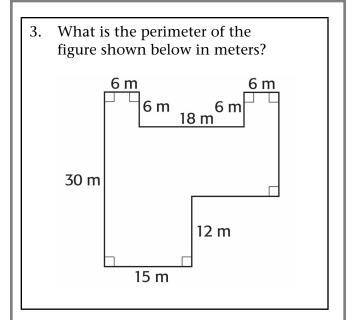
1.5 in.

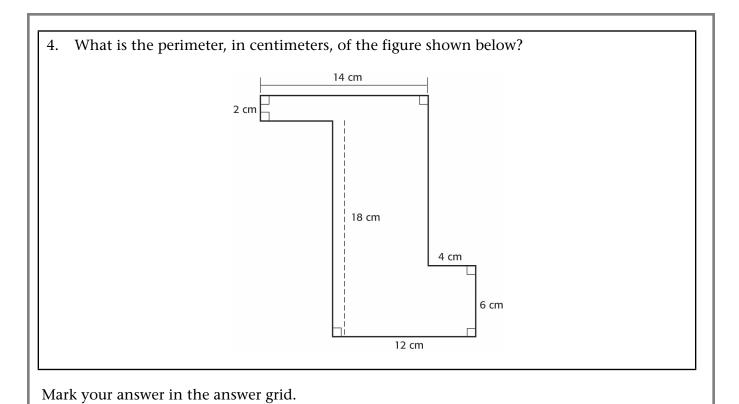
1.5 in.

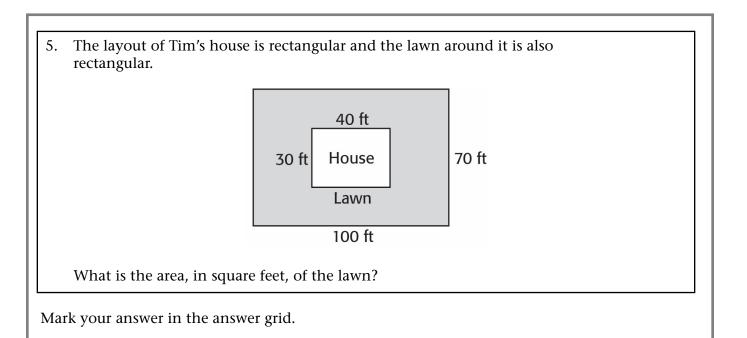
1.5 in.

What is the area, in square inches, of the remaining part of the original rectangle?

Mark your answer in the answer grid.







Sample Open-Ended Items

This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

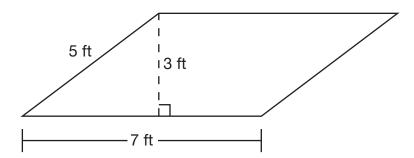
- 1. Jason is making a poster. He buys a piece of rectangular poster board that is 24 inches by 30 inches. From the piece of poster board, he is going to make two identical rectangular posters.
 - a. What is the *greatest* area each poster can have?
 - b. Using the entire poster board, how could Jason cut the poster board into two identical rectangles with the *least* perimeter?
 - c. Using the entire poster board, what is the *least* perimeter each poster can have?

This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

- 2. The top of the Traeger family's kitchen table is square. The Reyes family's kitchen tabletop is rectangular. The perimeter of each tabletop is 18 feet.
 - a. Draw and label an outline of the top of the Traeger's table.
 - b. Draw and label *one* possible outline of the top of the Reyes's table.
 - c. Which table has the greatest area?

This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

3. Frank has a rug in the shape shown below.



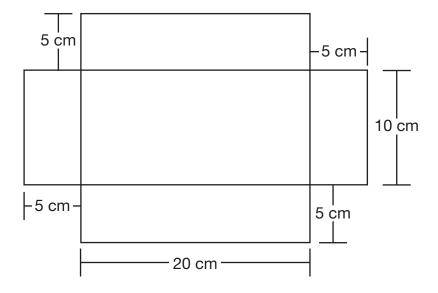
- a. What is the area, in square feet, of Frank's rug?
- b. What is the perimeter, in feet, of Frank's rug?
- c. Frank has a rectangular blanket with the same perimeter as the rug and a width of 3 feet. What is the length, in feet, of Frank's blanket?

This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

- 4. Darcy is drawing three different rectangles that each have a perimeter of exactly 24 inches.
 - a. The first rectangle has a length of 10 inches. What is the width of the first rectangle?
 - b. The second rectangle has an area of 35 square inches. What are the length and width of the second rectangle?
 - c. The third rectangle is a square. How many inches long is each side of the square?

This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

5. Jamar drew two figures using 5 rectangles that could be folded into an open box. The first figure is shown below.



- a. What is the total area, in square centimeters, of the 5 rectangles?
- b. Jamar's second figure had 5 squares that could be folded into an open box which had the same total area as the first figure. Each of the squares had the same area. What is the length, in centimeters, of each of the sides of the squares?
- c. What is the perimeter, in centimeters, of each of the squares in Jamar's second figure?

Answer Key

Content Standard 7

Sample Multiple-Choice

- 1. C
- 2. A
- 3. B
- 4. B
- **5.** C
- 6. C
- 7. D
- 8. B
- 9. C
- 10. C
- 11. A

Sample Gridded

- 1. 10.7
- 2. 98.7
- 3. 132
- 4. 76
- 5. 5800

Sample Open-Ended

1. Sample Response(s):

a. $24 \times 30 = 720$ and $720 \div 2 = 360$ square inches

OR

Equivalent

b. Jason can cut the poster in half either <u>vertically</u> or <u>horizontally</u>. (The more a rectangle approaches being a square, the smaller its perimeter.) Cutting 30 in half, rather than the 24, yields rectangles with a total perimeter that is less than the perimeter obtained by cutting the 24 in half.

$$P = 2l + 2w$$
. $2(24) + 2(\frac{30}{2}) = 78$ which is less than $2(\frac{24}{2}) + 2(30) = 84$

OR

Equivalent (may see labeled drawings of two rectangles)

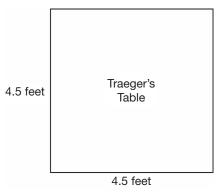
c. If Jason cuts the poster <u>horizontally</u>, he gets two rectangles. Each measures 12 by 30 with a perimeter of 2(12) + 2(30) = 84 inches. If he cuts the poster <u>vertically</u>, he gets two rectangles. Each measures 24 by 15 with a perimeter of 2(24) + 2(15) = 78 inches. 78 inches is less than 84 inches.

OR

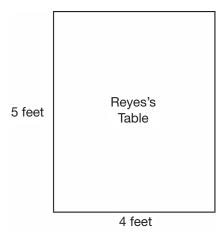
Score Point	Response Attributes	
3	All is correct.	
	All logics are correct.	
	OR	
2	Two correct logics and correct answers for one or more problems.	
	OR	
	One correct logic and correct answers for all problems.	
One or more answers to problems are correct without logic.		
1	OR	
	One logic is correct.	
0	None correct. (Also, blanks, rewrites problems, foreign language, illegible, refusals, off task, etc., scored as invalid.)	

2. Sample Response(s):

a. To find the Traeger's tabletop, $18 \div 4 = 4.5$. The square tabletop has dimensions of 4.5 feet by 4.5 feet.



b. The Reyes's tabletop, with perimeter 18, could be 5 feet by 4 feet, so that 5 + 4 + 5 + 4 = 18.



c. The Traeger's tabletop has an area of 4.5 feet \times 4.5 feet = 20.25 feet squared. The Reyes's tabletop has an area of 5 feet \times 4 feet = 20 feet squared. The Traeger's tabletop has the greater area.

Score Point	Response Attributes	
3	All is correct.	
	All logics are correct.	
2	OR Two correct logics and correct answers for one or more problems.	
	OR One correct logic and correct answers for all problems.	
One or more answers to problems are correct without logic.		
1	OR One logic is correct.	
0	None correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off-task, etc., scored as invalid.)	

3. Sample Response(s):

a. Area of parallelogram = base \times height = $7 \times 3 = 21$ square feet

OR

Equivalent

b. Perimeter of parallelogram = sum of lengths of sides = 5 + 7 + 5 + 7 = 24 feet

OR

Equivalent (may see $2 \times 5 + 2 \times 7$)

c. Since the width of the blanket is 3 ft. and the perimeter is 24 ft., the length must be 9 ft. because 3 + 9 + 3 + 9 = 24.

OR

Score Point	Response Attributes	
3	All is correct.	
	All logics are correct.	
2	OR Two correct logics and correct answers for one or more problems.	
	OR	
	One correct logic and correct answers for all problems.	
One or more answers to problems are correct without logic.		
1	OR	
	One logic is correct.	
0	None correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off-task, etc., scored as invalid.)	

4. Sample Response(s):

a. Since P = 2l + 2w, then 24 = 2(10) + 2w and 24 - 20 = 4 = 2w and $w = 4 \div 2 = 2$ inches for the width.

OR

Equivalent

b. A = lw = 35 and since 24 = 2l + 2w, then l + w = 12. I set up a guess and check table:

Length (in.)	Width (in.)	Area (sq. in.)
3	9	27
4	8	32
5 inches	7 inches	35

OR

Equivalent

c. Perimeter of a square = 4s = 24 and solving for s, one gets s = 24/4 = 6 inches

OR

Score Point	Response Attributes		
3	All is correct.		
	All logics are correct.		
	OR		
2	Two correct logics and correct answers for one or more problems or drawings.		
	OR		
	One correct logic and correct answers for all problems.		
	One or more answers to problems are correct without logic.		
1	OR		
	One logic is correct.		
0	None correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off-task, etc., scored as invalid.)		

5. Sample Response(s):

a. $2(5 \times 10) + 2(5 \times 20) + (10 \times 20) = 500$ square centimeters

OR

Equivalent

b. $500 = 5(l \times l) = 5 \times 10 \times 10$ so each side is 10 centimeters

OR

Equivalent

c. P = 4s = 4(10) = 40 centimeters

OR

Score Point	Response Attributes
3	All is correct.
	All logics are correct.
2	OR Two correct logics and correct answers for one or more problems.
	OR One correct logic and correct answers for all problems.
One or more answers to problems are correct without logic.	
1	OR One correct logic.
None correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off-task, etc., scored as invalid.)	

MEASUREMENT

Content Standard 8

Determine the distance between two points on a scale drawing or a map using proportional reasoning.

Item Type

Multiple-choice Gridded

Additional Information

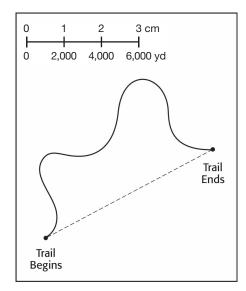
Determining the scale may be required. Scale drawing may be included. Word problems/real-life situations may be used. Measuring a scale drawing may be required.

Sample Multiple-Choice Items

1.	The ac	tual distan	ice from a	
	post of	fice to an	elementary	
	school	is 16.5 mi	les. A city	
	map u	ses a scale	of $\frac{1}{2}$ inch	
	represe	ents 15 mil	les.	
	the dis	tance, in i	nest represents nches, on the post office ary school?	I .
0	.55	1.1	1.65	3.3
	A *	В	C	D

2. Use your centimeter ruler and this map to help you answer this question.

The dotted-line segment on the map shows the shortest distance from the beginning of a hiking trail to the end of a hiking trail.

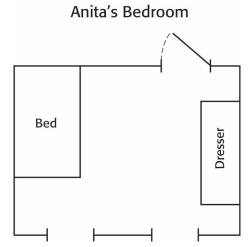


Which is *closest* to the actual distance, in yards, represented by the dotted-line segment?

500 5,000 10,000 25,000 **A B C** * **D**

The scale used to cr		centimeter represents 3 feet	
6 centimeters	6.75 feet B	9 centimeters	18 feet D *

4. A scale drawing of Anita's bedroom is shown below.



Anita used a scale of 1 centimeter represents 3 feet. Using your ruler, determine the actual dimensions of Anita's bedroom.

- **A** $4\frac{1}{2}$ centimeters by 6 centimeters
- **C** 13 $\frac{1}{2}$ feet by 18 feet *

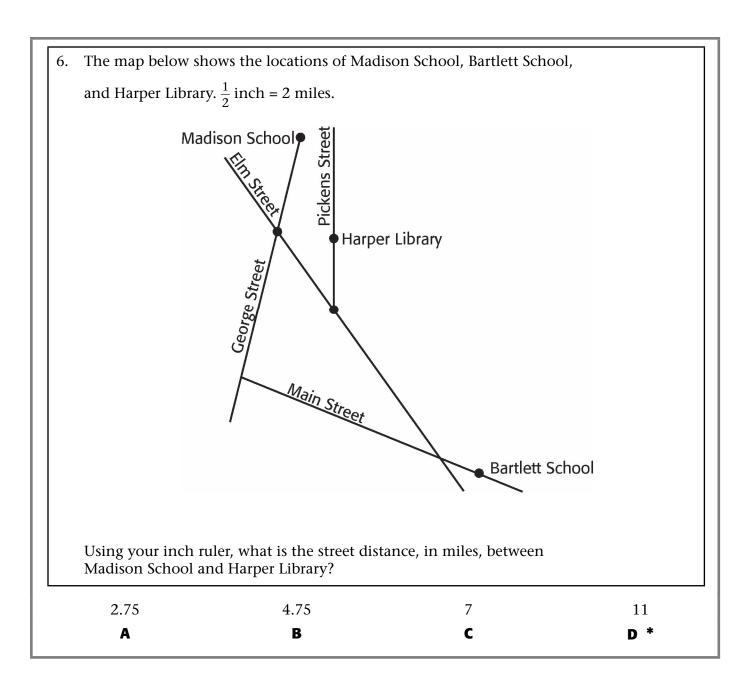
B 9 feet by 12 feet

D $13\frac{1}{2}$ meters by 18 meters

5. The actual distance from Jarret's home to Lake Mitchell is 140 miles. The distance on a map is 3.5 inches.

What scale could have been used for the map?

- **A** 1 inch = 4 miles
- **B** 1 inch = 40 miles *
- **C** 1 inch = 137.5 miles
- **D** 1 inch = 490 miles



Sample Gridded Items

1. The floor plan of the Murphy home uses a scale of 1 inch to represent 4 feet.

If the actual length of the Murphy living room is 18 feet, what is the length, in inches, on the floor plan?

Mark your answer in the answer grid.

2. Harold and Danielle each drew a scale drawing of a monument. In Harold's drawing, the height of the monument was 15 centimeters and the width was 6 centimeters. Danielle's drawing of the monument was similar to Harold's. In Danielle's drawing, the height of the monument was 20 centimeters.

What was the width of the monument, in centimeters, in Danielle's scale drawing?

Mark your answer in the answer grid.

Answer Key

Content Standard 8

Sample Multiple-Choice

- 1. A
- 2. C
- 3. D
- 4. C
- 5. B
- 6. D

Sample Gridded

- 1. 4.5
- 2. 8

MEASUREMENT

Content Standard 9

Convert units of length, weight, or capacity within the same system (customary or metric).

Item Type

Multiple-choice

Additional Information

Converting from a larger unit to a smaller unit may be required. Converting from a smaller unit to a larger unit may be required. Word problems/real-life situations may be used.

Sample Multiple-Choice Items

1. Henry's fish tank has a capacity of 28 quarts of water.

How many gallons of water would it take to fill Henry's fish tank to capacity?

- **A** 112 gallons
- C 7 gallons *
- **B** 28 gallons
- **D** 4 gallons

3. A bottle holds 1 pint of liquid.

Which of the following is equivalent to 1 pint?

- **A** 2 gallons
- C 2 quarts
- **B** 2 fluid ounces
- **D** 2 cups *

2. A bridge has a weight limit of 16,000 pounds.

What is the weight limit, in tons, of this bridge?

- **A** 8 tons *
- **C** 80 tons
- **B** 16 tons
- **D** 160 tons

Savannah is 155 centimeters tall.

Which of the following is equivalent to 155 centimeters?

- **A** 0.0155 m
- **C** 1.55 m *
- **B** 0.155 m
- **D** 15.5 m
- A bag of pecans that Alexis wants to buy has a total weight of 54 ounces.

Which of the following is equivalent to 54 ounces?

- **A** 6.75 pounds
- **C** 2.25 pounds
- **B** 3.375 pounds *
- **D** 1.125 pounds
- The package of crackers that Anna bought has a mass of 49 grams.

Which of the following is equivalent to 49 grams?

- **A** 4.9 kg
- **C** 0.049 kg *
- **B** 0.49 kg
- **D** 0.0049 kg

Armando jumped over a puddle of water that was 76 inches wide.

> Which of the following is equivalent, in feet, to the width of this puddle of water?

- **A** $7\frac{1}{2}$ feet **C** $6\frac{1}{4}$ feet
- **B** $6\frac{1}{3}$ feet *
- **D** $1\frac{1}{2}$ feet
- The length of the earthworm that Timmy found in his backyard was 38 millimeters.

Which is equivalent to 38 millimeters?

- **A** 0.038 cm
- **C** 3.8 cm *
- **B** 0.38 cm
- **D** 380 cm
- The phonebook for the city of Mapleton had a mass of 0.7 kilograms.

Which of the following is equivalent to 0.7 kilograms?

- **A** 70 grams
- **C** 7,000 grams
- **B** 700 grams *
- **D** 70,000 grams

10. David made 9 liters of fruit punch.

Which of the following is equivalent to 9 liters?

- **A** 0.9 milliliters
- **B** 9 milliliters
- **C** 90 milliliters
- **D** 9,000 milliliters *

11. Miguel ordered a total of 18 gallons of milk for his grocery store.

Which of the following is equivalent to 18 gallons?

- **A** 72 quarts *
- **B** 144 cups
- C 288 fluid ounces
- **D** 2,304 pints

Answer Key

Content Standard 9

Sample Multiple-Choice

- 1. C
- 2. A
- 3. D
- **4.** C
- 5. B
- 6. C
- 7. B
- 8. C
- 9. B
- 10. D
- 11. A

DATA ANALYSIS AND PROBABILITY

Content Standard 10

Interpret information from bar graphs, line graphs, and circle graphs.

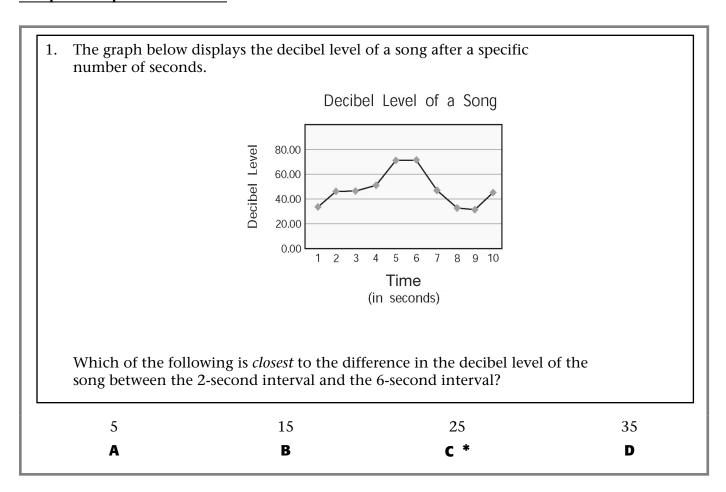
Item Type

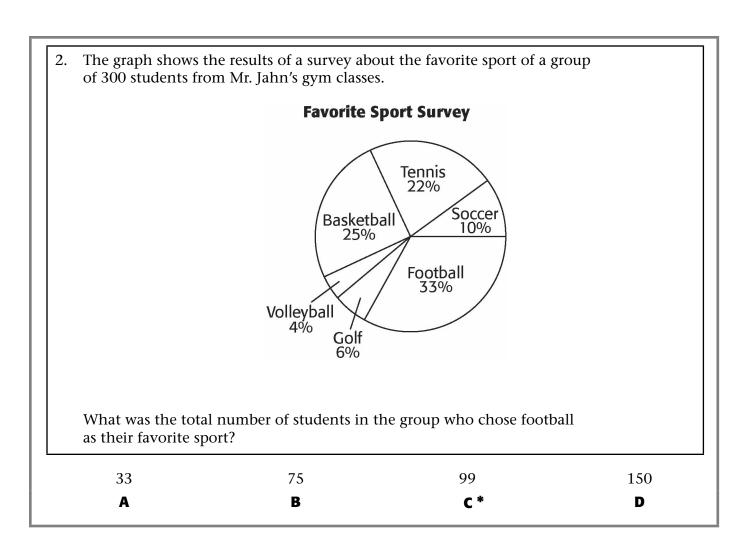
Multiple-choice Gridded Open-ended

Additional Information

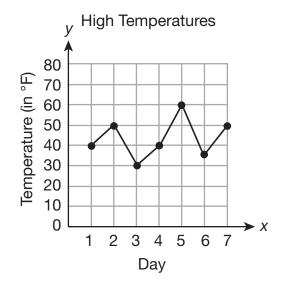
Word problems/real-life situations may be used.
Comparing types of graphs may be required.
Determining percents may be required.
Money values may be used.
In determining values in graphs, *closest* may be used.

Sample Multiple-Choice Items





3. Jenny recorded the high temperature each day for one week. She made the graph shown below.



Between which two days did the *greatest* change in temperature occur?

- **A** Day 2 to Day 3
- **B** Day 4 to Day 5
- C Day 5 to Day 6 *
- **D** Day 6 to Day 7

Sample Gridded Items

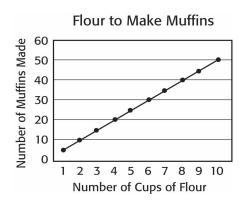
1. The graph below displays the sales amounts for puzzles over a number of years.



By how many dollars did the sales of puzzles increase from 1996 to 1998?

Mark your answer in the answer grid.

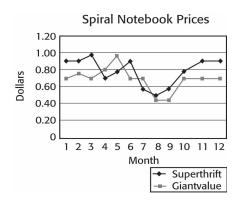
2. The line graph below displays the amount of flour needed in a muffin recipe.



Based on this graph, what is the number of cups of flour needed to make 40 muffins?

Mark your answer in the answer grid.

3. The graph below displays the price of spiral notebooks at two different stores over a 12-month period.



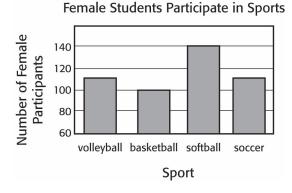
Which month appears to have had the *least* difference in price of spiral notebooks at the two stores?

Mark your answer in the answer grid.

Sample Open-Ended Items

This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

1. In the school newsletter there is an article about the number of female students who participate in sports at the school. The data display shown in the article shows that softball is twice as popular among the female students as basketball.



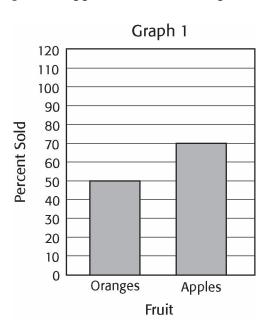
- a. Would you accept this data display and interpretation? Why or why not?
- b. Draw a graph that would accompany the article. Explain why you chose this graph.

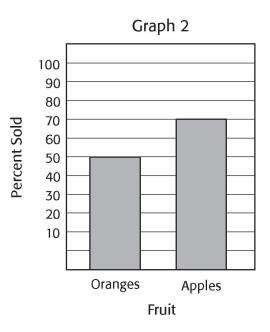
This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

2. The number of oranges and apples sold at a produce stand are shown in this table.

	Number	Number
	Displayed	Sold
Oranges	70	35
Apples	90	63

Mrs. Valdez wants to use one of the graphs below to display the percent of oranges and apples she sold in her produce stand.





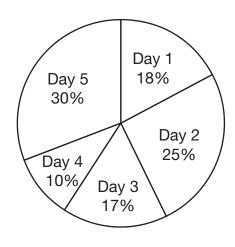
- a. Does one bar graph more accurately present the data than the other bar graph?
- b. In a sentence or two, state how the less accurate bar graph could be changed so that it would better represent the data in the table.

This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

3. Mr. Hansen recorded the number of students who ate sandwiches at lunch each day for 5 days. He used the data to create the 2 graphs shown below.

Students Who Ate Sandwiches 45 40 Number of Students 35 30 25 20 15 10 5 5 0 1 2 3 4 Day

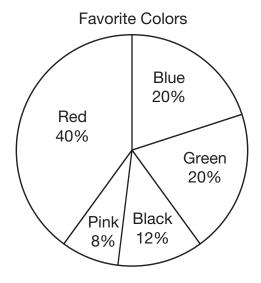
Students Who Ate Sandwiches



- a. What is the *closest* estimate of the total number of students who ate sandwiches?
- b. How many more students ate sandwiches on day 3 than on day 4?
- c. Explain why it is easier to use the bar graph than the circle graph to find how many more students ate sandwiches on day 5 than on day 3.

This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

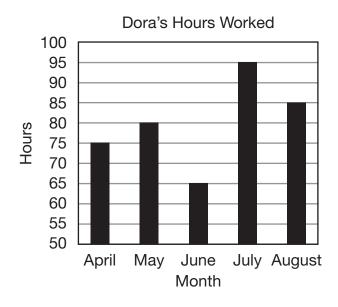
4. The circle graph below shows the favorite colors of students in Mr. Hendrick's class. Each student chose only one color.



- a. Which color was chosen by *fewer* students than those who chose blue but by *more* students than those who chose pink?
- b. David said that 16 students chose red. Explain why this *may* be true.
- c. Give one reason why the circle graph is a better way to represent the data than a line graph.

This problem requires you to show all your work or explain all your reasoning. You may use drawings, words, or numbers in your answer. Your answer should be written so that another person could read it and understand your reasoning.

5. Dora recorded the number of hours she worked each month in the bar graph shown below.



- a. Which month did Dora work the *greatest* number of hours?
- b. How many total hours did Dora work in the five months?
- c. Based on the graph, Dora said she worked three times as many hours in July as she worked in June. Explain why Dora is *not* correct.

Answer Key

Content Standard 10

Sample Multiple-Choice

- 1. C
- 2. C
- 3. C

Sample Gridded

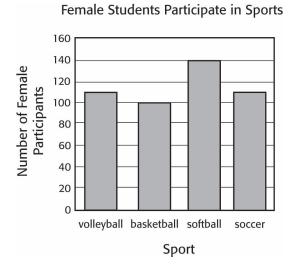
- 1. \$150000 or \$150000.00 or 150000 or 150000.00
- 2. 8
- 3. 8

1. Sample Response(s):

a. I would not accept this graphic because the intervals make it visually misleading. The vertical axis does not start at zero, and the difference between softball and basketball participation appears to be more substantial than it actually is.

A better representation would include a bar graph or a circle graph drawn to scale.

b.



I chose this graph to illustrate the information in the article because a bar graph works well for this type of representation. In the original question, the vertical axis was wrong. It needs to start at zero as mine does, so that the graph does not look like softball is twice as popular as basketball.

Score Point	Response Attributes	
3	All is correct.	
2	All logics are correct. OR One logic and graph are correct.	
1	One logic is correct. OR The graph has no more than three errors.	
0	None correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off-task, etc., scored as invalid.)	

2. Sample Response(s):

- a. Graph 1 displays the data more accurately than Graph 2. Graph 2 is misleading, because the first interval on the *y*-axis is much larger than all the other intervals. This makes the number of oranges sold appear much closer to the number of oranges displayed.
- **b.** How the student could possibly better the less accurate graph will vary. Students might possibly state that the vertical axis should have all the same sized intervals beginning at zero.

Score Point	Response Attributes	
3	All is correct.	
2	All logics are correct.	
1	One logic is correct. OR Correct answer for part b.	
0	None correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off-task, etc., scored as invalid.)	

3. Sample Response(s):

a. 27 + 38 + 25 + 15 + 45 = 150 (students who ate sandwiches)

OR

Equivalent

b. 25 - 15 = 10 (more students who ate sandwiches)

OR

Equivalent

c. The bar graph better represents the data as it can actually give you the number of students who ate sandwiches each day, whereas the circle graph only gives percentages and one would need to know the total number of students who ate sandwiches for all five days, then multiply by the percentage difference of day 5 and day 3. (The bar graph is much more direct or efficient.)

OR

Score Point	Response Attributes		
3	All is correct.		
	All logics are correct.		
	OR All of part a and all of part b are correct.		
2	OR Part c is correct and two correct answers.		
	OR One correct logic for part a, part c is correct, and correct answer for either part a or b.		
	One or more answers to problems are correct without logic.		
1	OR One logic is correct.		
0	None correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off-task, etc., scored as invalid.)		

4. Sample Response(s):

- **a.** Black (12%)—it is the only color represented on the graph that is between Pink (8%) and Blue (20%).
- **b.** It is not the <u>number</u> of students that is being recorded in the circle graph, but the <u>percentage</u> of students who chose a certain color. If there were 40 students in the class, then 40% of 40 means that 16 students chose red.

OR

Equivalent

c. A circle graph compares parts to a whole while a line graph does not. Line graphs show actual numbers but more computation is necessary to make a comparison.

OR

Score Point	Response Attributes
3	All is correct.
	Two logics are correct.
2	OR One logic and one answer are correct.
	One answer is correct without logic.
1	OR One logic is correct.
0	None correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off-task, etc., scored as invalid.)

5. Sample Response(s):

- **a.** July—it is the tallest bar on the graph.
- **b.** 75 + 80 + 65 + 95 + 85 = 400 (hours worked)

OR

Equivalent

c. The bar graph reads 65 hours worked for June and 95 hours worked for July. Ninety-five is not 3 times as much as 65.

OR

Dora would have needed to work 195 hours in July to work three times as many hours. She only worked 95 hours.

OR

Dora did not take into account the "y-axis break." July's bar *appears* to be three times as tall as June's bar, but neither bar shows the first 50 hours worked that are a part of all five bars shown.

OR

Score Point	Response Attributes
3	All is correct.
	Two logics are correct.
2	OR Part c is correct and correct answer for part a or part b.
	One or more answers to problems are correct without logic.
1	OR One correct logic.
0	None correct. (Also, blanks, rewrites problem, foreign language, illegible, refusals, off-task, etc., scored as invalid.)

DATA ANALYSIS AND PROBABILITY

Content Standard 11

Find the probability of a simple event.

Item Type

Multiple-choice Gridded

Additional Information

Expressing probability as a fraction, decimal, or percent may be required. Tables may be used.

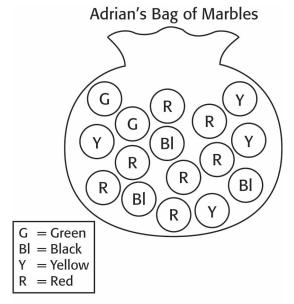
Word problems/real-life situations may be used.

Diagrams may be included.

Sample Multiple-Choice Items

There are 9 yellow tiles, 6 green tiles, 6 blue tiles, and 3 red tiles in a box. All the tiles in the box are identical in size and shape. What is the probability that the first tile picked at random from the box will be red? 12.5% 25.0% 37.5% 50.0% A * В C D

2.	The picture below represents Adrian's bag of marbles. All of the marbles
	are the same size and shape.



What is the probability that Adrian will *not* select a yellow or red marble, without looking, on his first try?

 $\frac{3}{10}$

 $\frac{7}{10}$

 $\frac{5}{16}$

 $\frac{5}{32}$

Α

В

C *

D

3. Trudie is playing a game with identical-sized colored sticks. She has a container with a total of 10 red, 12 green, 19 blue, and 9 yellow sticks.

If Trudie picks a stick without looking, what is the probability the stick will be green?

12% 24% 76% 88%

A B* C D

4. There are 12 students playing a game that requires each one to pick a piece of paper from a hat. The pieces of paper are identical in size, and on each of the pieces is the name of a different student playing the game.

What is the probability that a student will pick the piece of paper from the hat with his or her own name?

 $\frac{1}{12}$ $\frac{6}{12}$ $\frac{7}{12}$ $\frac{8}{12}$ **A** * **B C D**

5. A game has 9 red cards, 4 blue cards, and 7 gold cards. A card is picked at random.

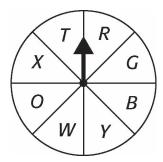
What is the probability that the card picked is a blue card?

0.02 0.04 0.2 0.4

A B C* D

Sample Gridded Items

1. The spinner below is divided into 8 equal sections. Whitney spun the arrow on the spinner once.



If Whitney spins the arrow once, what is the probability that the spinner will *not* land on *T*?

Express your answer as a decimal.

Mark your answer in the answer grid.

2. Maryanne painted some identical-sized wooden blocks. She painted 6 green wooden blocks, 5 red wooden blocks, 4 blue wooden blocks, and 5 yellow wooden blocks and placed them in an empty bag.

If Maryanne then selects a wooden block from the bag without looking, what is the probability that it will be one that was painted red?

Express your answer as a decimal.

Mark your answer in the answer grid.

3. A citywide youth event had participants from four neighborhoods. There were 250 participants from Oak Bluff, 310 participants from Gordon Grove, 280 participants from Riverside, and 160 participants from Webster Heights.

If a participant is chosen at random to win a prize, what is the probability that the participant will be from Gordon Grove?

Express your answer as a decimal.

Mark your answer in the answer grid.

5. Angela put colored paperclips into her empty pocket. She put 13 pink, 4 red, 1 yellow, and 2 green paperclips into her pocket. All of the paperclips are the same size and shape.

If Angela reaches into her pocket containing these colored paperclips and selects a paperclip, what is the probability it will be a green or yellow paperclip?

Express your answer as a decimal.

Mark your answer in the answer grid.

4. Brendan has 40 individual socks in his drawer. Of all the socks, 26 are dark blue.

If Brendan opens the drawer and selects one sock without looking, what is the probability that he will select a sock that is *not* dark blue?

Express your answer as a decimal.

Mark your answer in the answer grid.

6. Mrs. Tapper selected a helper for science class by writing each of the students' names on a piece of paper and selecting one at random. There were 13 boys and 15 girls in the class.

What is the probability that a boy was selected?

Express your answer as a fraction.

Mark your answer in the answer grid.

Answer Key

Content Standard 11

Sample Multiple-Choice

- 1. A
- 2. C
- 3. B
- 4. A
- 5. C

Sample Gridded

- 1. 0.875
- 2. 0.25
- 3. 0.31
- 4. 0.35
- 5. 0.15
- 6. 13/28

SAMPLE RESPONSE FORMAT

SAMPLE RESPONSE: MULTIPLE-CHOICE

Page _____

1	A	B	©	D
2	A	B	©	(D)
3	A	B	©	D
4	A	B	©	(D)
5	A	B	© © © ©	D

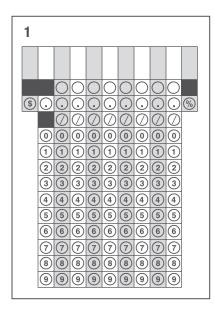
Page _____

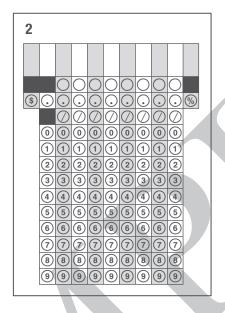
6	A	B	©	(D)
7	A	lacksquare	©	D
8	A	B	©	D

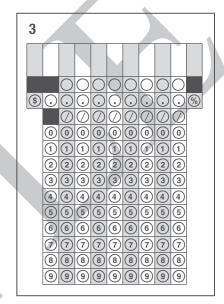
Page ____

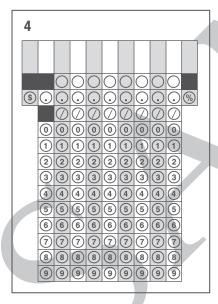
9	A	lacksquare	©	(D)
10	A	B	©	(D)

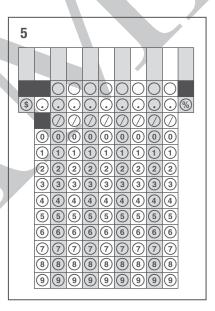
SAMPLE RESPONSE: GRIDDED



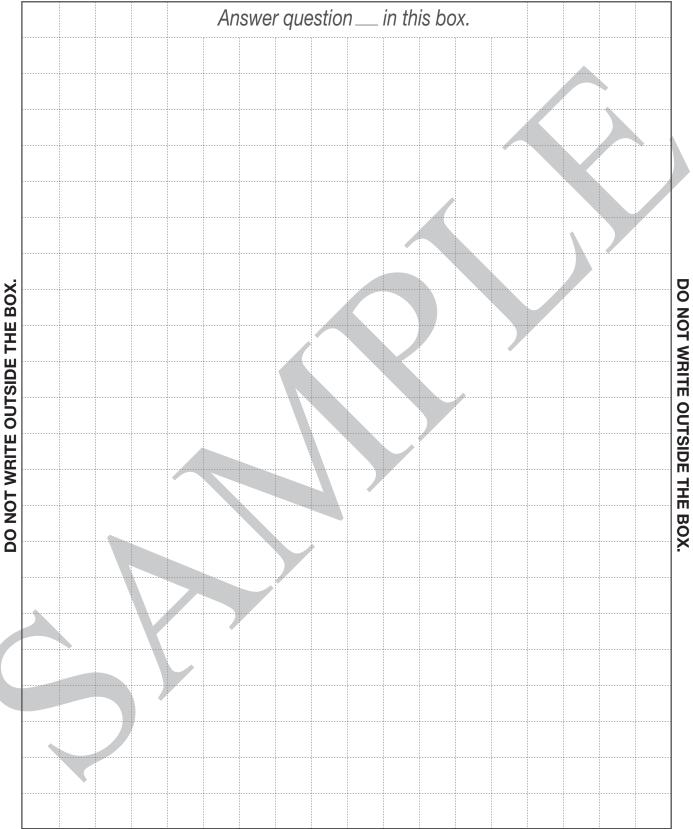








SAMPLE RESPONSE: OPEN-ENDED
Be sure to leave room in your answer space for all parts of this test question.



DO NOT WRITE OUTSIDE THE BOX.